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Ab initio properties of Li-group-II molecules for ultracold matter studiesSvetlana Kotochigova,^{1,a)} Alexander Petrov,^{1,b)} Maria Linnik,¹ Jacek Kłos,² and Paul S. Julienne³¹*Department of Physics, Temple University, Philadelphia, Pennsylvania 19122, USA*²*Department of Chemistry and Biochemistry, University of Maryland, College Park, Maryland 20742, USA*³*Joint Quantum Institute, NIST and University of Maryland, Gaithersburg, Maryland 20899-8423, USA*

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We perform a systematic investigation of the electronic properties of the $^2\Sigma^+$ ground state of Li-alkaline-earth dimers. These molecules are proposed as possible candidates for quantum simulation of lattice-spin models. We apply powerful quantum chemistry coupled-cluster method and large basis sets to calculate potential energies and permanent dipole moments for the LiBe, LiMg, LiCa, LiSr, and LiYb molecules. Agreement of calculated molecular constants with existing experimental data is better than or equal to 8%. Our results reveal a surprising irregularity in the dissociation energy and bond length with an increase in the reduced mass of the molecule. At the same time, the permanent dipole moment at the equilibrium separation has the smallest value between 0.01 a.u. and 0.1 a.u. for the heaviest (LiSr and LiYb) molecules and increases to 1.4 a.u. for the lightest (LiBe), where 1 a.u. is one atomic unit of dipole moment. We consider our study of the $^2\Sigma^+$ molecules a first step towards a comprehensive analysis of their interactions in an optical trap. © 2011 American Institute of Physics. [doi:10.1063/1.3653974]

I. INTRODUCTION

There is growing interest in molecules formed by one alkali-metal atom and one alkaline-earth or rare-earth atom.¹⁻¹¹ In contrast to group I or group II di-atomic molecules, these molecules have an unpaired electron that allows for manipulation of the $X^2\Sigma^+$ ground-state molecule with both electric and magnetic external fields. Moreover, it has been suggested that $^2\Sigma^+$ molecules are good candidates in which controlled chemical reactions can be explored at ultracold temperatures.¹² The unpaired spin in the ground state of these molecules should provide a new handle for the control of the reaction dynamics based on the interplay between intramolecular spin-rotation couplings. In addition, when placed in an optical lattice, these polar molecules can interact with each other via both electric dipole-dipole and magnetic spin-spin forces. It is therefore possible to engineer unusual forms of interactions for quantum simulation of lattice-spin models and topological quantum computing,¹ controlled preparation of many-body entangled states,⁴ and high-precision measurements of fundamental constants.¹³

Another interest in Li-group II molecules stems from prospects to achieve optical Feshbach tuning of scattering properties in ultracold gases of the individual atoms without substantial loss of atoms from a trap. This photoassociative tuning, pioneered for homonuclear molecules,¹⁴⁻²¹ becomes possible due to the existence of long-lived excited molecular states near narrow intercombination lines of the alkaline-earth or rare-earth atoms. In turn, this might enable efficient ways to form gases of polar molecules without substantial loss

by photoassociation. In essence, a two-photon optical Feshbach resonance can be used to couple two colliding atoms to a vibrational level of the molecular ground state. The suppressed effect of excited-state spontaneous decay makes efficient coherent molecular formation possible. Knowledge of the electronic and rovibrational properties of the molecules will help to find optimal pathways. Characteristics such as the permanent dipole moments of the ground state will determine the anisotropic interactions between these molecules in an optical trap.

Some key theoretical predictions of the electronic structure and dipole moment of the ground and low-lying excited states of LiYb^{8,9} and for the ground state of LiSr⁶ have recently been obtained. Another work has studied RbYb² and RbSr.⁵ However, the physical origin of the chemical bond of these mixed species is not yet fully understood. Continued theoretical advances are necessary to unravel the properties of these molecular systems. To the best of our knowledge, only the LiMg and LiCa ground states were experimentally investigated,^{11,22,23} which allow us to compare our predictions with experimentally obtained molecular parameters.^{11,23} There are several experimental groups working to achieve the formation of the LiYb molecules at ultracold temperatures.^{7,10} An understanding and quantitative description of these molecules might help to define conditions under which these ultracold molecular systems can be created.

Our theoretical study is devoted to a systematic investigation of the $X^2\Sigma^+$ ground state properties of the polar Li-alkaline-earth diatoms such as LiBe, LiMg, LiCa, LiSr, and the rare-earth diatoms LiYb. These are interesting and challenging systems as the valence electrons of the atoms form a relatively weak covalent bond.²⁴ The alkaline-earth atom has a closed outer electron shell and a Hartree-Fock interaction

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energy results in a purely repulsive potential curve. We use the unrestricted (U) or partially spin-restricted (R) coupled cluster (CC) method with either single and double excitations augmented with perturbatively calculated triples (CCSD(T)) or with single, double, and triple excitations (CCSDT) to treat the correlations of core and valence electrons. All approaches are used in conjunction with correlation-consistent basis sets. The dipole moment is calculated using a finite field approach with a four-point numerical differentiation formula. The calculations are performed with CFOUR²⁵ and MOLPRO²⁶ suites of programs.

Presumably, the CCSDT method is more accurate in the description of the potential energy surface than the CCSD(T) method, where triple excitations are treated perturbatively. The results of the unrestricted (U) method are more accurate than that of a restricted (R) calculation. The CC method is based on a single-reference configuration and is not suitable for molecules where multiple-configurations are relevant. A practical indicator of how well the CC method performs is based on T1 diagnostics.²⁷ Our calculation shows that T1 is small and varies from 0.015 to 0.035. This indicates that a single-reference method is valid for these diatoms. In fact, a small T1 for all interatomic separations implies that the long-range interaction potentials as well as the dissociation energies can be accurately described.

Our results include the ground-state potential curve, bond distance, harmonic frequency, dissociation energy, and permanent dipole moment for LiBe, LiMg, LiCa, LiSr, and LiYb. For completeness, we calculate vibrational energies of the ground-state potentials. Due to limitations in computational resources, we were not able to obtain results for all methods, basis sets, and Li-X diatoms. The most accurate potential energy curves and dipole moments are presented in the figures and tables with the exception of Table VI, which compares molecular constants obtained with the various methods and basis sets.

All potentials are corrected for basis set superposition errors (BSSE) using the counterpoise procedure of Boys and Bernardi.³² The sign of the dipole moment depends on the position of the origin. We apply the following convention throughout the paper. The alkaline-earth/rare-earth atom is positioned at the origin and the Li atom moves along the positive x axis. A positive sign of the dipole moment corresponds to the charge transfer from the Li atom towards the alkaline-earth/rare-earth atom.

A. LiBe molecule

There exist several theoretical calculations of the $X^2\Sigma_{1/2}^+$ electronic ground state of the LiBe molecule. Jones²⁸ used a density functional formalism based on a local density approximation to predict molecular constants of the LiBe, LiMg, and LiCa molecules. Their dissociation energy is $D_e/(hc) = 3705.9 \text{ cm}^{-1}$, while the equilibrium bond length R_e is $4.9a_0$ and the vibrational constant $\omega_e/(hc) = 340 \text{ cm}^{-1}$. Such strong bonding of the LiBe molecule was explained by substantial electron-charge transfer between s and p orbitals. More advanced multi-reference configuration interaction (MRCI) calculations of the low-lying doublet and quartet

states of LiBe was performed by Fischer *et al.*²⁹ In this calculation, the ground state is bound by 2497.5 cm^{-1} , $R_e = 4.95a_0$, and $\omega_e/(hc) = 302 \text{ cm}^{-1}$. The permanent dipole moment is $d_e = 0.95 \text{ a.u.}$ at R_e . Another MRCI calculation²⁴ using all single and double excitations obtained $D_e/(hc) = 2336.35 \text{ cm}^{-1}$, $R_e = 4.927a_0$, and $\omega_e/(hc) = 300 \text{ cm}^{-1}$, which are close to those of Ref. 29. However, the dipole moment $d_e = 1.33 \text{ a.u.}$ of Ref. 24 differs significantly from that of Ref. 29. The effect of inner-shell correlations on the molecular electronic structure was investigated. Later an *ab initio* configuration-interaction study was reported by Marino and Ermler.³⁰ Their value of the dissociation energy $D_e/(hc) = 2014 \text{ cm}^{-1}$ is smaller than that in previous studies. In summary, the previous theoretical calculations disagree on dissociation energy and dipole moment values but have much better agreement on the value of the bond length. Our goal is to test results of the previous predictions by performing a coupled cluster calculation accounting for high-order correlation effects.

In our calculation, the UCCSD(T) method is used to obtain the ground-state potential and dipole moment of LiBe as a function of interatomic separation R . These characteristics are calculated with the large basis set (aug-cc-pV5Z-DK) of Prascher *et al.*,³⁴ which includes scalar relativistic effects accounted for by the Douglas-Kroll Hamiltonian. Atomic basis sets include (15s8p5d4f3g2h) primitive Gaussian and [7s6p5d4f3g2h] constructed functions for Li and (15s9p5d4f3g2h)/[7s6p5d4f3g2h] for Be.

Results of our calculation are shown in Fig. 1. Comparing our data with results available from other theories and experiment, we conclude that $R_e = 4.87a_0$ is close to the experimental measurement of $R_e = 4.894a_0$,³¹ while the well depth $D_e/(hc) = 2406.89 \text{ cm}^{-1}$ is in best agreement with the prediction of Ref. 24. In Ref. 31, no value of D_e is given. The dipole moment value $d_e = 1.41 \text{ a.u.}$ at the equilibrium separation

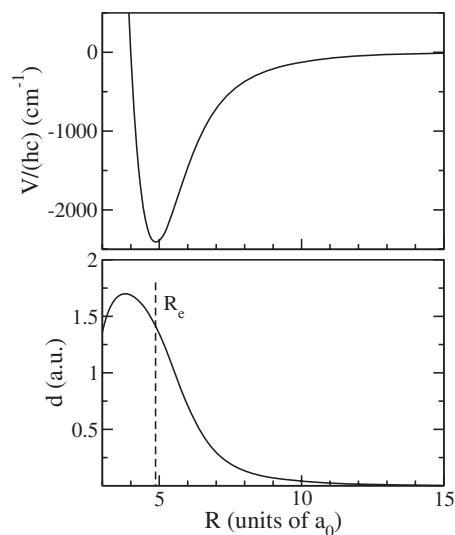


FIG. 1. Top panel: electronic $^2\Sigma^+$ ground-state potential of LiBe; bottom panel: permanent dipole moment function of the ground state of LiBe. The vertical dashed line indicates the equilibrium separation of the ground-state potential, at which the dipole moment equals 1.41 a.u. The vibrationally averaged dipole moment of the $v = 0$ level is equal to a slightly smaller value of 1.372 a.u.

TABLE I. All vibrational energies of the ${}^7\text{Li}{}^9\text{Be}$ $X^2\Sigma^+$ ground-state potential for the rotational state $N = 0$.

ν	Energy/(hc) (cm^{-1})	ν	Energy/(hc) (cm^{-1})
0	-2254.29	9	-337.24
1	-1954.76	10	-243.42
2	-1669.25	11	-169.45
3	-1407.21	12	-112.19
4	-1167.64	13	-68.88
5	-951.37	14	-37.48
6	-760.21	15	-16.55
7	-594.38	16	-4.86
8	-453.64	17	-0.50

is even larger than that of Ref. 24. The permanent dipole moment averaged over the ground state vibrational wave function is equal to 1.37 a.u. It is slightly lower than the value of the dipole moment function at $R = R_e$. The LiBe molecule has the largest dipole moment of the molecular systems considered in this work.

Bound states of ${}^7\text{Li}{}^9\text{Be}$ are calculated using a discrete variable representation (DVR),³⁵ and their binding energies are presented in Table I. The zero-point energy is found to be $D_0/(hc) = 2254.29 \text{ cm}^{-1}$.

B. LiMg molecule

To the best of our knowledge, there exist two experimental investigations of the LiMg ground-state properties.^{22,23} The study in Ref. 23 provides molecular constants that we can use for comparison with our calculation. This work was based on resonant photo-ionization spectroscopy of LiMg in the gas phase and gives an accurate bond energy $D_0/(hc) = 1330 \text{ cm}^{-1}$, equilibrium separation $R_e = 5.9a_0$, and vibrational frequency $\omega_e/(hc) = 190 \text{ cm}^{-1}$. A density functional study in Ref. 28 of LiMg gives $D_e/(hc) = 1371 \text{ cm}^{-1}$, $R_e = 6.04a_0$, and $\omega_e/(hc) = 180 \text{ cm}^{-1}$. A MRCI approach with large contracted basis sets and multiple sets of polarization functions is used in Ref. 24 to give predictions for the LiMg ground state molecular constants $D_e/(hc) = 1611.28 \text{ cm}^{-1}$, $R_e = 5.88a_0$, and $\omega_e/(hc) = 183 \text{ cm}^{-1}$. The value for D_e significantly differs from both Ref. 28 and experiment.

Here we apply RCCSD(T) and UCCSD(T) methods with two different basis sets to calculate the potential and dipole moment of the LiMg ground state. Augmented polarized core-valence (aug-cc-pCVQZ) basis sets with Li:(15s9p5d3f1g)/[8s7p5d3f1g] and Mg:(19s15p6d4f2g)/[9s8p6d4f2g] functions^{33,34} are used to calculate the ground-state potential energy at the RCCSD(T) level of theory, where all electrons in both Li and Mg are correlated. Aug-cc-pv5z-DK basis sets with Li:(14s8p4d3f2g1h)/[6s5p4d3f2g1h] and Mg:(20s14p4d3f2g1h)/[7s6p4d3f2g1h] (Ref. 34) are applied in the UCCSD(T) calculation. The calculation is optimized for scalar relativistic calculations of the all-electron Douglas-Kroll Hamiltonian. A comparison with the molecular constants measured in Ref. 23 shows that our D_0 and R_e

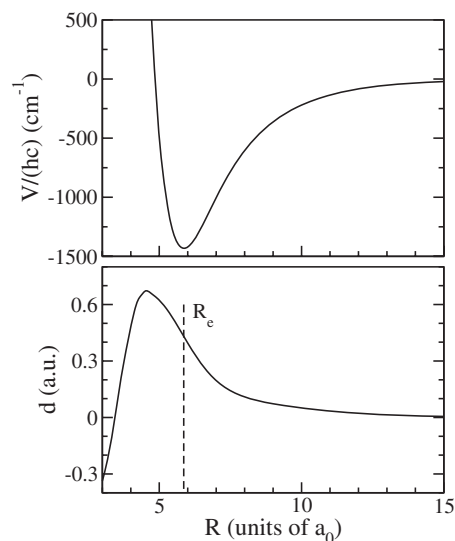


FIG. 2. Top panel: electronic $X^2\Sigma^+$ ground-state potential of LiMg; bottom panel: permanent dipole moment, where a vertical dashed line indicates the equilibrium separation of the ground-state potential. There the dipole moment is 0.44 a.u., while the vibrationally averaged value for the $\nu = 0$ level is 0.413 a.u.

values are in good agreement with this experiment. Figure 2 shows the R -dependent potential and dipole moment.

In Table II, we present a complete list of $N = 0$ bound states of the $X^2\Sigma^+$ ground-state potential of ${}^7\text{Li}{}^{24}\text{Mg}$ obtained by a DVR calculation. The zero-point corrected energy is found to be $D_0/(hc) = 1330.05 \text{ cm}^{-1}$ in agreement with experimental measurement.²³

C. LiCa molecule

Currently, there is no reliable experimental data for the ground-state potential of the LiCa molecule in the literature. However, preliminary experimental results on the electronic properties of the ground-state LiCa potential based on high resolution spectroscopy were presented at the EGAS conference in 2010.¹¹ They gave the molecular constants $D_e/(hc) = 2607.8(100) \text{ cm}^{-1}$, $R_e = 6.3415(5)a_0$, and $\omega_e/(hc) = 195.2 \text{ cm}^{-1}$ for ${}^7\text{Li}{}^{40}\text{Ca}$. Earlier theoretical predictions

TABLE II. All vibrational energies of the ${}^7\text{Li}{}^{24}\text{Mg}$ $X^2\Sigma^+$ ground-state potential for the $N = 0$ rotational state. The potential is based on the RCCSD(T) calculation.

ν	Energy/(hc) (cm^{-1})	ν	Energy/(hc) (cm^{-1})
0	-1330.05	10	-216.21
1	-1164.35	11	-164.06
2	-1010.96	12	-120.16
3	-870.00	13	-83.91
4	-741.52	14	-54.87
5	-625.41	15	-32.62
6	-521.43	16	-16.78
7	-429.16	17	-6.89
8	-348.00	18	-1.75
9	-277.27	19	-0.12

for the LiCa ground state give a dissociation energy of $D_e/(hc) = 2177.7 \text{ cm}^{-1}$ and $R_e = 6.65a_0$ using density functional theory.²⁸ Later a configuration-interaction calculation involving an effective pseudo-potential³⁷ predicted $D_e/(hc) = 2355 \text{ cm}^{-1}$ and $R_e = 6.23a_0$. An all-electron *ab initio* study of LiCa in Ref. 38 reported $D_e/(hc) = 1935.7 \text{ cm}^{-1}$ and $R_e = 6.44a_0$. Experimental two-photon ionization spectroscopy reported in the same work found that R_e equals to $6.3865a_0$. The substantial discrepancy in the reported characteristics and lack of the experimental data on the electronic structure of this molecule has initiated our study.

An accurate treatment of the LiCa molecule with presumably weak bonding requires a massive inclusion of correlation effects. To satisfy this requirement, we apply two coupled-cluster approaches, UCCSD(T) and UCCSDT, that allow us to introduce higher-order correlation effects. To probe the influence of basis sets on the LiCa characteristics, we used two different basis sets for each atom. These are all-electron basis sets with quadruple-zeta quality. Basis sets (def2-QZVPP) for Li:(15s6p2d1f)/[6s4p2d1f] and Ca:(24s18p6d3f)/[11s6p4d3f] functions are taken from Ref. 40. Basis sets (aug-cc-pCVQZ) with Li:(15s9p5d3f1g)/[8s7p5d3f1g] and Ca:(25s19p10d4f2g)/[10s9p7d4f2g] functions^{33,36} include larger correlation expansions.

We find that the molecular characteristics depend not only on the basis set but also on the number of correlated electrons n_{el} . For example, for a three-electron correlation, one $2s^1$ valence electron of Li and two $4s^2$ valence electrons of Ca are correlated, whereas for 13-electron correlation, all electrons of Li and ten $3s^23p^64s^2$ electrons of Ca are included in the active space. We conclude that using the UCCSD(T) method and the more advanced basis set (aug-cc-pCVQZ) leads to an increase of $D_e/(hc)$ and d_e by $\approx 5\%$. For the UCCSDT method, we expect similar trends. We believe that the UCCSDT calculation with the basis set (aug-cc-pCVQZ) provides the most accurate electronic potential and dipole moment. These are shown in Fig. 3. Moreover, this calculation is in a good agreement with the experimental molecular constants reported by Ref. 11.

The upper panel of Fig. 3 shows the potential energy curve of the $X^2\Sigma^+$ state of LiCa as a function of interatomic separation. The permanent dipole moment of this state as a function of R is presented in the lower panel. A complete list of the $N = 0$ vibrational energies of the ground state is presented in Table III.

D. LiSr molecule

To our knowledge there exist no data on the LiSr ground-state potential based on experimental observation. We are only able to compare our results to the theoretical results of Ref. 6. The calculation of Ref. 6 uses an effective core and core polarization potentials that are incorporated in a configuration-interaction approach. Their molecular constants are $R_e = 6.57a_0$, $D_e/(hc) = 2587 \text{ cm}^{-1}$, $\omega_e/(hc) = 184.9 \text{ cm}^{-1}$, $B_e/(hc) = 0.21 \text{ cm}^{-1}$, and $d_e = 0.13 \text{ a.u.}$ In the present study, we use different computational methods to predict these characteristics.

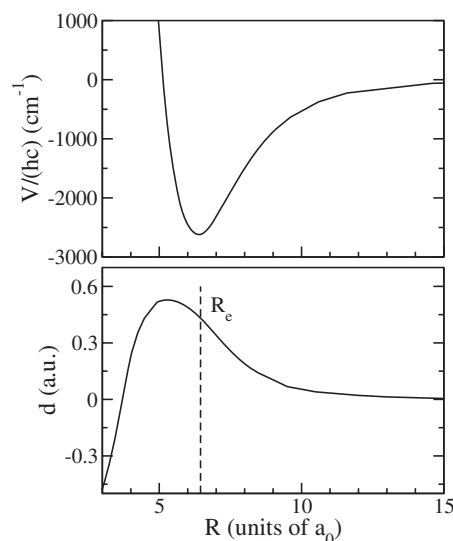


FIG. 3. Top panel: electronic ground state $^2\Sigma_{1/2}^+$ potential of LiCa; bottom panel: permanent dipole moment of the ground state of LiCa. The vertical dashed line indicates the equilibrium separation of the ground-state potential. At this separation the dipole moment is 0.044 a.u. The vibrationally averaged dipole moment with the $v = 0$ wave function is 0.437 a.u.

We perform calculations for LiSr that are similar to those for LiCa. We use UCCSD(T) and UCCSDT methods with three different basis sets. The inner electrons of the closed $1s^22s^2 \dots 3d^{10}$ shells of Sr are chemically inactive and excluded from the correlation calculation. The $1s^22s^1$ electrons of Li and the ten $5s^24s^24p^6$ electrons of Sr are included in the all-order correlation calculation.

In the first calculation, we use the basis set def2-QZVPP with Li:(15s6p2d1f)/[6s4p2d1f] and Sr:(8s8p5d3f)/[7s5p4d3f] functions⁴⁰ and the Stuttgart ECP28MDF relativistic effective core potential (ECP).³⁹ In a second calculation, we use the basis set of Ref. 41 with Li: (14s8p4d2f)/[7s6p4d2f] and Sr:(14s11p5d4f1g)/[8s8p5d4f1g] functions. The effective core potential is

TABLE III. All vibrational energies of the $^7\text{Li}^{40}\text{Ca } X^2\Sigma^+$ ground-state potential for the rotational state $N = 0$. The potential is based on the UCCSD(T)/aug-cc-PCVQZ calculation.

v	Energy/(hc) (cm^{-1})	v	Energy/(hc) (cm^{-1})
0	-2428.02	14	-442.18
1	-2232.09	15	-366.32
2	-2042.75	16	-298.77
3	-1861.87	17	-239.22
4	-1688.77	18	-187.31
5	-1524.31	19	-142.70
6	-1368.30	20	-105.03
7	-1221.05	21	-73.95
8	-1082.74	22	-49.08
9	-953.39	23	-30.02
10	-833.10	24	-16.33
11	-721.92	25	-7.41
12	-619.79	26	-2.47
13	-526.60	27	-0.42

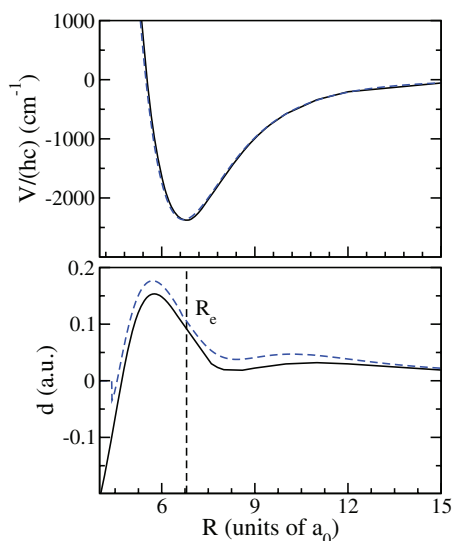


FIG. 4. Top panel: electronic ground-state ${}^2\Sigma^+$ potential of LiSr; bottom panel: permanent dipole moment of the ground-state of LiSr. The potentials and dipole moments are obtained by two different methods: UCCSDT (solid curve) and UCCSD(T) (dashed curve). The vertical dashed line in the bottom panel indicates the equilibrium separation of the ground-state potential. The vibrationally averaged dipole moment with the $\nu = 0$ wave function is 0.111 a.u.

from Ref. 41. Finally, we performed a calculation with a more advanced all-electron basis set (aug-cc-pCV5Z) described by Li:(18s12p7d5f3g1h)/[10s9p7d5f3g1h] and Sr:(23s19p12d4f2g)/[11s10p7d4f2g] functions from Ref. 34. The UCCSDT calculation is time consuming and has been performed for basis set of Ref. 41 only.

Results of the most advanced calculation by the UCCSDT method with the basis set of Ref. 41 and the UCCSD(T) method with basis set (aug-cc-pCV5Z) are shown in Fig. 4. We see that the potential energy of the two calculations nearly coincide, whereas the dipole moment curves in the bottom panel are slightly shifted relative to each other. We believe that this difference is within the accuracy of our calculation. The largest discrepancy of about 7% with the results of Ref. 6 occurs at large internuclear separation, whereas at R_e the dipole moment d_e differs by 2%–3% only.

The DVR calculation of the bound state energy gives $D_0/(hc) = 2275.59 \text{ cm}^{-1}$ and $\omega/(hc) = 182.2 \text{ cm}^{-1}$. Table IV lists all $N = 0$ bound-state energies for ${}^7\text{Li}^{88}\text{Sr}$.

E. LiYb molecule

Recently, two extensive quantum-chemical calculations of the ground and excited states of the LiYb molecule have been reported by Zhang *et al.*⁸ and by Gopakumar *et al.*⁹ The first calculation used both MRCI and UCCSD(T) methods. Scalar relativistic effects were included by the Douglas-Kroll Hamiltonian and an effective core potential. Their molecular constants for the $X^2\Sigma^+$ ground state of ${}^7\text{Li}^{172}\text{Yb}$ are as follows: $R_e = 6.681a_0$, $D_e/(hc) = 1577 \text{ cm}^{-1}$, and $\omega_e/(hc) = 147.36 \text{ cm}^{-1}$. Different treatments of the Yb core electrons lead to different values of the dipole moment. A RECP-pseudo-potential calculation gave $d_e = 0.022 \text{ a.u.}$, while an

TABLE IV. All vibrational energies of the ${}^7\text{Li}^{88}\text{Sr } X^2\Sigma^+$ ground-state potential for the rotational state $N = 0$. The potential is based on the UCCSD(T) calculation with basis set.³⁴

ν	Energy/(hc) (cm^{-1})	ν	Energy/(hc) (cm^{-1})
0	-2275.59	15	-397.78
1	-2099.56	16	-331.60
2	-1931.06	17	-272.33
3	-1769.35	18	-219.76
4	-1614.41	19	-173.66
5	-1466.66	20	-133.76
6	-1326.14	21	-99.83
7	-1192.91	22	-71.56
8	-1067.12	23	-48.65
9	-948.89	24	-30.80
10	-838.24	25	-17.64
11	-735.17	26	-8.73
12	-639.65	27	-3.42
13	-551.65	28	-0.86
14	-471.08	29	-0.04

all-electron DKH3 calculation gave a smaller d_e of 0.011 a.u. Results of a calculation by Ref. 9 were based on both the CASPT2 perturbation theory and the CCSD(T) method. Relativistic effects were taken into account through the Douglas-Kroll-Hess Hamiltonian. Their best values of molecular constants are: $R_e = 6.669a_0$, $D_e/(hc) = 1421.96 \text{ cm}^{-1}$, and $\omega_e/(hc) = 135.54 \text{ cm}^{-1}$.

Our goal here is to perform an independent calculation of the ground-state potential and permanent dipole moment of LiYb using the UCCSD(T) method with another effective ECP28MWB pseudo-potential and with basis sets for Li:(15s6p2d1f)/[6s4p2d1f] and Yb:(14s13p10d8f6g)/[10s8p5d4f3g] functions from Ref. 42.

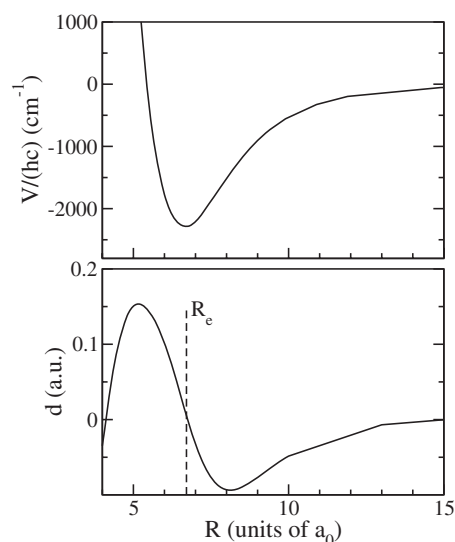


FIG. 5. Top panel: electronic ground-state ${}^2\Sigma^+$ potential of LiYb; bottom panel: permanent dipole moment of the ground state. The vertical dashed line in the bottom panel indicates the equilibrium separation of the ground-state potential.

TABLE V. All vibrational energies of the ${}^7\text{Li}^{172}\text{Yb } X^2\Sigma^+$ ground-state potential for the rotational state $N = 0$. The potential is based on the UCCSD(T) calculation with basis set.⁴²

ν	Energy/(hc) (cm^{-1})	ν	Energy/(hc) (cm^{-1})
0	-2277.12	16	-349.63
1	-2103.98	17	-289.41
2	-1938.15	18	-235.73
3	-1778.86	19	-188.38
4	-1626.11	20	-147.10
5	-1480.30	21	-111.67
6	-1341.45	22	-81.82
7	-1209.63	23	-57.26
8	-1084.99	24	-37.70
9	-967.64	25	-22.84
10	-857.62	26	-12.36
11	-754.90	27	-5.66
12	-659.49	28	-1.94
13	-571.36	29	-0.36
14	-490.44	30	-0.005
15	-416.57		

Results of our calculation are shown in Fig. 5. The upper panel of Fig. 5 shows the ground-state potential of LiYb, which is significantly deeper than the potentials obtained in Refs. 8 and 9. The permanent dipole moment is presented in the bottom panel. It is small and agrees well with the DKH3 value of Ref. 8.

Table V shows all $N = 0$ bound-state energies for ${}^7\text{Li}^{172}\text{Yb}$.

II. SUMMARY

The objective of our research has been a systematic investigation of the $X^2\Sigma^+$ ground-state properties of Li-group II molecules. To achieve this goal we applied powerful quantum chemistry UCCSD(T) and UCCSDT methods with large basis sets to calculate potential energies and permanent dipole moments. Table VI displays molecular constants obtained in our calculations.

Figures 6 and 7 and Table VI summarize our results. Figure 6 reveals a most striking irregularity in the dissociation energy and R_e among the Li-group II molecules. The deepest and most shallow potentials belong to the LiCa and LiMg molecules, respectively.

Figure 7 shows dipole moment functions for all molecules considered in our study. There is some consistency in the maximum value of d with the reduced mass of the molecule: heavier molecules have smaller dipole moment. The dipole moment averaged over the ground state vibrational wave function is always a few tenths of atomic units smaller than d_e . The LiSr and LiYb molecules have the smallest dipole moments among all molecules in this study.

Table VI presents molecular constants calculated by the RCCSD(T), UCCSD(T), and UCCSDT methods using several large basis sets available in the literature. Comparison of our most accurate (either UCCSD(T) or UCCSDT) calculations with existing experimental measurements of the

TABLE VI. Molecular constants for the $X^2\Sigma^+$ state of LiBe, LiMg, LiCa, LiSr, and LiYb obtained by the RCCSD(T), UCCSD(T), and UCCSDT methods. Here, $1 a_0 = 0.0529177$ nm is the Bohr radius and a dipole moment of 1 a.u. corresponds to $1 ea_0$, where e is the electron charge. Also h is Planck's constant and c the speed of light.

Description	R_e (a_0)	$\omega_e/(hc)$ (cm^{-1})	$D_e/(hc)$ (cm^{-1})	d_e (a.u.)
${}^7\text{Li}^9\text{Be}$				
UCCSD(T)				
aug-cc-pV5Z-DK	4.873	299.5	2406	1.41
Experiment (Ref. 31)	4.894			
${}^7\text{Li}^{24}\text{Mg}$				
RCCSD(T)				
aug-cc-pCVQZ	5.86	174.4	1417	0.32
UCCSD(T)				
aug-cc-pV5Z-DK	5.87	206.1	1432	0.44
Experiment (Ref. 23)	5.9	190	1423 ^a	
${}^7\text{Li}^{40}\text{Ca}$				
UCCSD(T)				
def2-QZVPP	6.410	196.0	2320	0.438
aug-cc-pCVQZ	6.358	205.5	2460	0.456
UCCSDT				
aug-cc-pCVQZ	6.357	207.1	2607	0.440
Experiment (Ref. 11)	6.3415(5)	195.2	2607.8(100)	
${}^7\text{Li}^{88}\text{Sr}$				
UCCSD(T)				
def2-QZVPP	6.766	167.0	2165	0.109
basis of Ref. 41	6.712	183.0	2302	0.117
aug-cc-pCV5Z	6.700	182.2	2367	0.112
UCCSDT				
basis of Ref. 41	6.711	184.2	2401	0.096
${}^7\text{Li}^{172}\text{Yb}$				
UCCSD(T)				
basis of Ref. 42	6.710	181.5	2289	0.011

^aThis value is estimated from D_0 of Ref. 23.

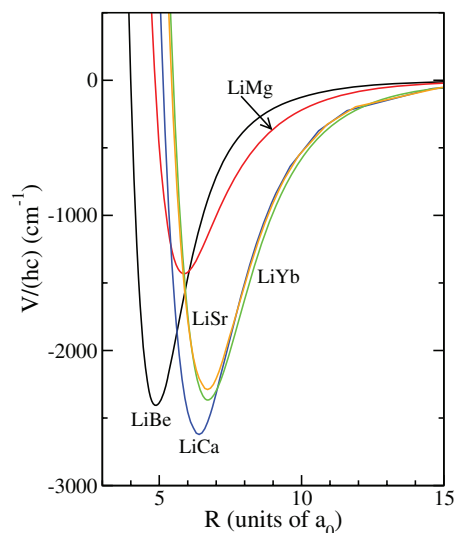


FIG. 6. Electronic ground-state ${}^2\Sigma^+$ potentials of Li-group II molecules and LiYb as a function of interatomic separation.

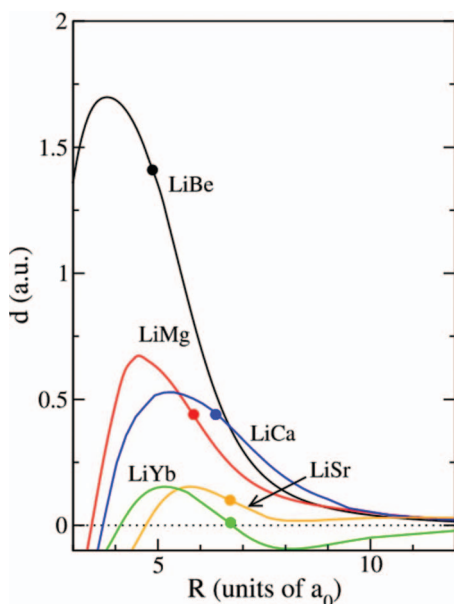


FIG. 7. Permanent dipole moment of the ground state of the Li-group II molecules and LiYb as a function of interatomic separation. Filled circles indicate dipole moment values at equilibrium separations of corresponding molecules.

molecular constants shows that we are able to reproduce the bond length (R_e), harmonic frequency (ω_e), and dissociation energy (D_e) within 5%, 8%, and 6%, respectively.

The dipole moment as a function R is calculated in terms of a charge transfer and induced charge transfer. These two contributions have opposite signs over a large range of inter-nuclear separations. We conclude from our calculations that charge transfer from the Li-atom to the alkaline-earth atom prevails at all separations. This trend is reversed for LiYb at $R > 7a_0$.

We also highlight the importance of the correlation effects in calculations of the alkali-alkaline-earth molecules. We have gathered numerical evidence to show that molecular constants of these molecules, such as dissociation energy and permanent dipole moment of the ground state, are extremely sensitive to high order correlations. We believe that the best values of these characteristics are obtained by using the UCCSDT method, where correlation effects are taken into account at all orders.

Finally, we want to emphasize that LiBe and LiMg are not likely candidates for ultracold studies because of the difficulty of cooling Be or Mg. However, LiCa looks quite promising, since a Ca BEC (Ref. 43) has been made, and its dipole moment is comparable to the known RbCs case.⁴⁴ The $2^2\Sigma^+$ ground state gives an extra spin degree of freedom relative to the $1^2\Sigma^+$ RbCs species, thus more quantum control possibilities. While ultracold Li + Sr and Li + Yb mixtures are possible for making the molecules, the dipole moments of the ground state molecules are rather modest. It remains to be determined how best to make the molecules from the trapped atoms. One possibility is to make “preformed pairs” in a dual species optical lattice,^{45,46} and then use intercombination line photoassociation followed by STIRAP.⁴⁷ Although all of these molecular species are expected to be highly chemical reactive in their ground states since the formation of the diatoms is exothermic

LiCa might have a large enough dipole moment to allow it to be protected against destructive collisions by aligning it with an electric field in a 1D optical lattice.^{1,48,49}

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